

Chapter 1 Review for Final

Date _____ Period _____

Identify a pattern and find the next three numbers in the pattern.

1) $-4, -1, 2, 5, \dots$ $8, 11, 14$

$\begin{matrix} \vee & \vee & \vee \\ +3 & +3 & +3 \end{matrix}$

2) $3, 21, 147, 1029, \dots$ $7203, 50421, 352947$

$\begin{matrix} \vee & \vee & \vee \\ \times 7 & \times 7 & \times 7 \end{matrix}$

State what sets of numbers the following numbers belong to.

3) -10 *integer, rational, real*

4) $-\frac{3}{4}$ *rational, real*

5) π *irrational, real*

6) $\sqrt{2}$ *irrational, real*

Simplify the expressions given that $a = 3$, $b = -4$ and $c = -10$

7) $2a + 3b$

$2(3) + 3(-4)$

-10

8) $-c + 2(a + b)$

$-(-10) + 2(3 + (-4))$

8

9) $-b^2 + a(c - 8)$

$-(-4)^2 + 3(-10 - 8)$ -70

10) $a^2 + 2b^2 - c^2$

$3^2 + 2(-4)^2 - (-10)^2$

$9 + 32 - 100$ -59

Solve each equation.

11) $-2(7 - x) = 2$

$-14 + 2x = 2$

$2x = 16$

$x = 8$

13) $2(1 + 7b) = -33 + 7b$

$2 + 14b = -33 + 7b$

$7b = -35$

$b = -5$

12) $-19 = -2(8 + n) + 3n$

$-19 = -16 - 2n + 3n$

$-19 = -16 + n$

$-3 = n$

14) $-8(2v - 5) = 8(4 - 3v) + 8v$

$-16v + 40 = 32 - 24v + 8v$

$8 = 0v$

$8 = 0$

~~no solution~~

no solution

15) $|-2 - 3n| + 2 = 10$

$|-2 - 3n| = 8$

$-2 - 3n = 8 \quad -2 - 3n = -8$

$-3n = 10 \quad -3n = -6$

$n = \frac{-10}{3}, 2$

16) $|2 - 4a| = 38$

$2 - 4a = 38$

$2 - 4a = -38$

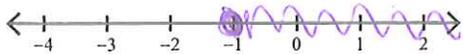
$-4a = 36$

$-4a = -40$

$a = -9, 10$

Solve each inequality and graph its solution.

17) $3(5k + 5) \geq 0$

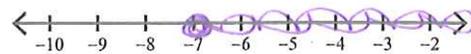


$$15k + 15 \geq 0$$

$$15k \geq -15$$

$$k \geq -1$$

18) $-(3p + 2) + 5p \geq -16$



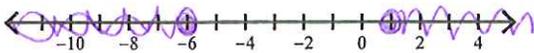
$$-3p - 2 + 5p \geq -16$$

$$2p \geq -14$$

$$p \geq -7$$

Solve each compound inequality and graph its solution.

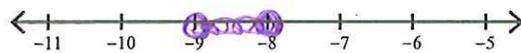
19) $5x \geq 5$ or $x + 4 \leq -2$



$$5x \geq 5 \quad \text{or} \quad x + 4 \leq -2$$

$$x \geq 1 \quad \text{or} \quad x \leq -6$$

20) $-54 \leq 6n \leq -48$

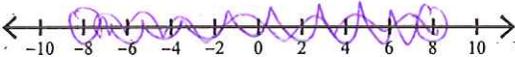


$$-54 \leq 6n \text{ and } 6n \leq -48$$

$$-9 \leq n \text{ and } n \leq -8$$

Solve each inequality and graph its solution.

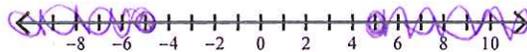
21) $\left| \frac{x}{2} \right| < 4$



$$\frac{x}{2} < 4 \quad \frac{x}{2} > -4$$

$$x < 8 \quad x > -8$$

22) $|4x| - 7 \geq 13$



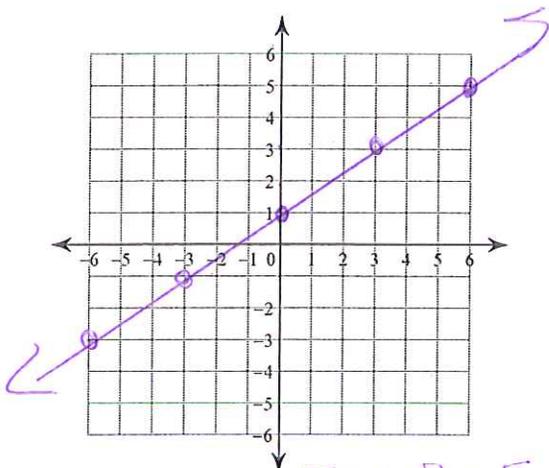
$$4x \geq 20 \quad 4x \leq -20$$

$$x \geq 5 \quad x \leq -5$$

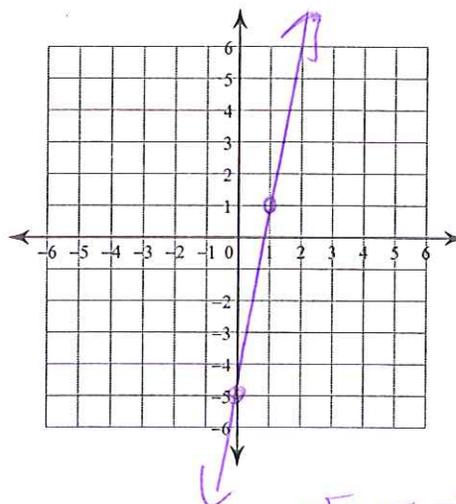
Chapter 2- Review for Final

Sketch the graph of each line.

1) $y = \frac{2}{3}x + 1$

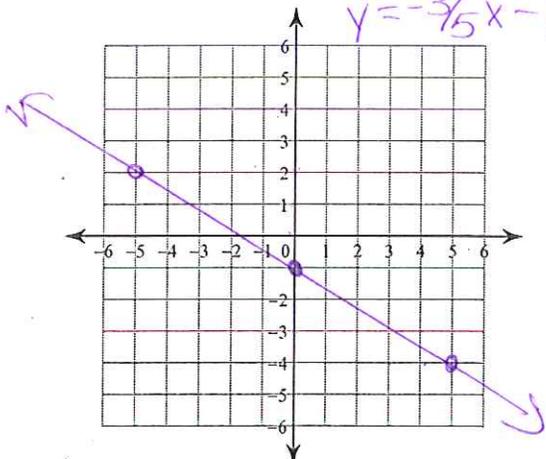


2) $y = 6x - 5$



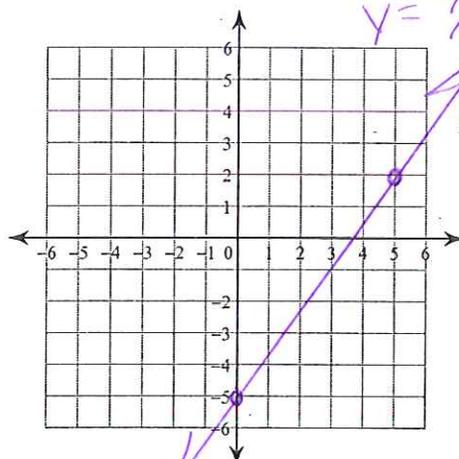
3) $3x + 5y = -5$

$5y = -3x - 5$
 $y = -\frac{3}{5}x - 1$



4) $7x - 5y = 25$

$-5y = -7x + 25$
 $y = \frac{7}{5}x - 5$



Write the slope-intercept form of the equation of each line given the slope and y-intercept.

5) Slope = 3, y-intercept = -3

$y = 3x - 3$

6) Slope = -2, y-intercept = -2

$y = -2x - 2$

Write the slope-intercept form of the equation of each line.

7) $5x + 3y = -15$

$3y = -5x - 15$

$y = -\frac{5}{3}x - 5$

8) $8x - 7y = 14$

$-7y = -8x + 14$

$y = \frac{8}{7}x - 2$

Write the slope-intercept form of the equation of the line through the given point with the given slope.

9) through: $(5, 3)$, slope = $\frac{8}{5}$
 $y - 3 = \frac{8}{5}(x - 5)$
 $y - 3 = \frac{8}{5}x - 8$
 $y = \frac{8}{5}x - 5$

10) through: $(-3, -3)$, slope = $-\frac{2}{3}$
 $y + 3 = -\frac{2}{3}(x + 3)$
 $y + 3 = -\frac{2}{3}x - 2$
 $y = -\frac{2}{3}x - 5$

Write the slope-intercept form of the equation of the line through the given points.

11) through: $(-1, -4)$ and $(0, 2)$
 $m = \frac{2 - (-4)}{0 - (-1)} = \frac{6}{1}$
 $y = 6x + 2$

12) through: $(0, -1)$ and $(-4, -2)$
 $m = \frac{-2 - (-1)}{-4 - 0} = \frac{-1}{-4} = \frac{1}{4}$
 $y = \frac{1}{4}x - 1$

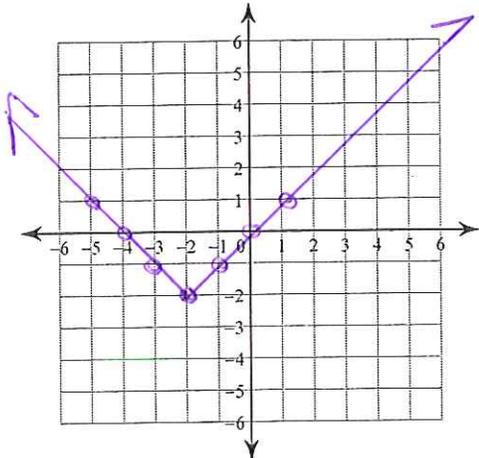
Write the point-slope form of the equation of the line described.

13) through: $(-2, 1)$, parallel to $y = \frac{3}{2}x - 5$
 $y - 1 = \frac{3}{2}(x + 2)$

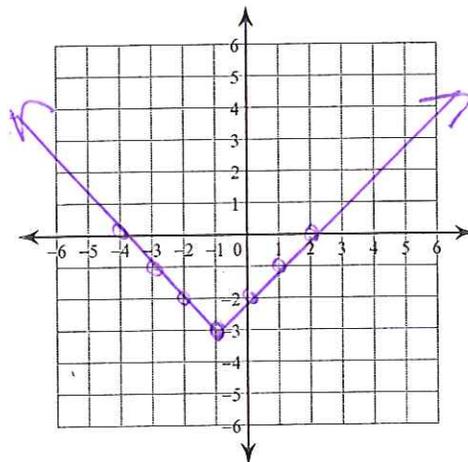
14) through: $(-2, 5)$, perp. to $y = \frac{3}{5}x - 3$
 $y - 5 = -\frac{5}{3}(x + 2)$

Graph each equation.

15) $y = |x + 2| - 2$

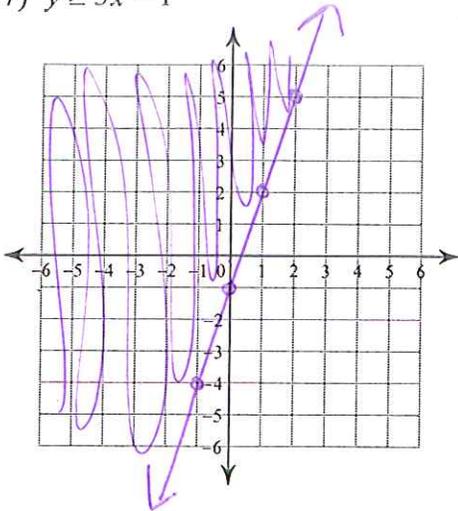


16) $y = |x + 1| - 3$

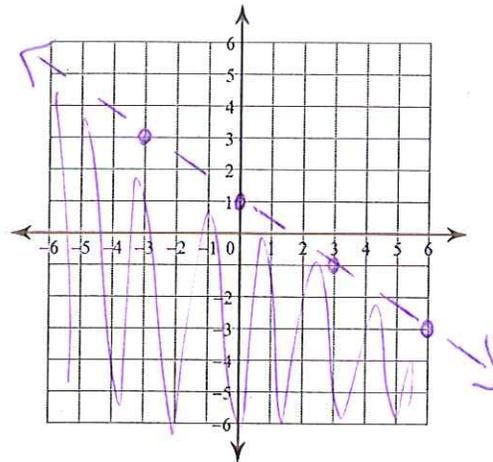


Sketch the graph of each linear inequality.

17) $y \geq 3x - 1$



18) $y < -\frac{2}{3}x + 1$



Evaluate each function.

19) $g(x) = -x^2 + x$; Find $g(5)$

$$g(5) = -(5)^2 + 5$$

$$\boxed{g(5) = -20}$$

20) $h(n) = -2n - 4$; Find $h(7)$

$$h(7) = -2(7) - 4$$

$$h(7) = -14 - 4$$

$$\boxed{h(7) = -18}$$

Determine if the following relations are functions.

21) $\{(2, 4), (7, -11), (8, 6), (7, 14)\}$

no because the input 7 has 2 outputs, -11 & 14

22) $\{(1, -3), (4, 9), (-16, -3), (11, 56)\}$

yes because each input has exactly one output.

Write an expression to model the following situations.

23) A tree is five feet tall and grows 2 feet each year.

$$5 + 2x$$

24) Jill has 25 dollars and spends 3 dollars a day on lunch.

$$25 - 3x$$

Chapter 3- Review for Final

Solve each system by substitution.

1) $6x + 5y = -7$
 $x - 8y = -10$
 $x = 8y - 10$

$6(8y - 10) + 5y = -7$
 $48y - 60 + 5y = -7$
 $53y = 53$
 $y = 1$

$x = 8(1) - 10$
 $x = -2$

$(-2, 1)$

Solve each system by elimination.

2) $10x - 2y = 20$
 $20x - 10y = 10$
 $-20x + 4y = -40$

$-6y = -30$
 $y = 5$

$10x - 2(5) = 20$
 $10x = 30$
 $x = 3$

$(3, 5)$

3) $6x + 4y = 2$
 $4(-9x + 3y) = -12$

$-18x - 12y = -6$
 $-36x + 12y = -48$

$-54x = -54$
 $x = 1$

$(1, -1)$

$6(1) + 4y = 2$
 $4y = -4$
 $y = -1$

4) $-6x + 3y - 6z = -21$
 $-x + 6y + 3z = -19$
 $5x - 6y - z = 17$

① $-6x + 3y - 6z = -21$
 ③ $5x - 6y - z = 17$
 $-12x + 6y - 12z = -42$

④ $-7x - 13z = -25$

② $-x + 6y + 3z = -19$
 ③ $5x - 6y - z = 17$

⑤ $4x + 2z = -2$

④ $-7x - 13z = -25$
 ⑤ $4x + 2z = -2$

② $-(-2) + 6y + 3(3) = -19$
 $6y = -30$
 $y = -5$
 $(-2, -5, 3)$

5) $6x + 5y + 4z = 6$
 $-2x - y - 4z = 10$
 $4x + 5y + 4z = 2$

$-23x - 52z = -100$
 $23x + 14z = -14$
 $-38z = -114$
 $z = 3$

⑤ $4x + 2(3) = -2$
 $4x + 6 = -2$
 $4x = -8$
 $x = -2$

① $6x + 5y + 4z = 6$
 ② $-2x - y - 4z = 10$

④ $4x + 4y = 16$

② $-2x - y - 4z = 10$
 ③ $4x + 5y + 4z = 2$

⑤ $2x + 4y = 12$

④ $4x + 4y = 16$
 ⑤ $-2x - 4y = -12$
 $2x = 4$
 $x = 2$
 $(2, 2, -4)$

⑤ $2(2) + 4y = 12$
 $4y = 8$
 $y = 2$

② $-2(2) - 2 - 4z = 10$
 $-6 - 4z = 10$
 $-4z = 16$
 $z = -4$

6) Carlos and Molly are selling fruit for a school fundraiser. Customers can buy small boxes of tangerines and large boxes of tangerines. Carlos sold 7 small boxes of tangerines and 12 large boxes of tangerines for a total of \$270. Molly sold 6 small boxes of tangerines and 2 large boxes of tangerines for a total of \$74. Find the cost each of one small box of tangerines and one large box of tangerines.

$x =$ cost of a small box
 $y =$ cost of a large box

$7x + 12y = 270$
 $-6(6x + 2y = 74)$
 $-36x - 12y = -444$
 $-29x = -174$
 $x = 6$

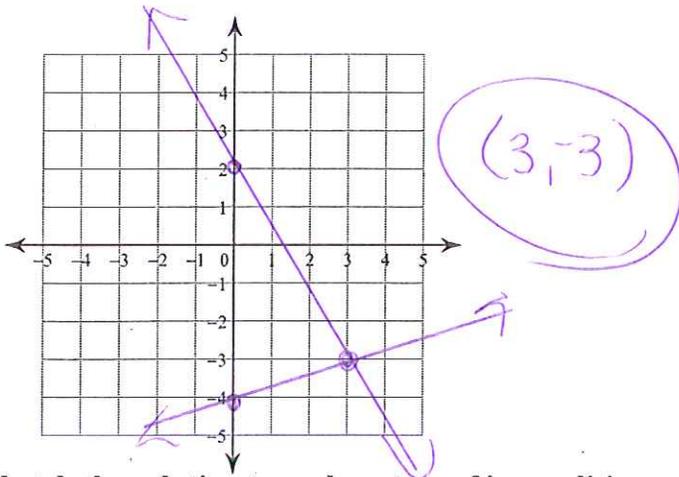
$7(6) + 12y = 270$
 $12y = 228$
 $y = 19$

-1- A small box costs \$6 and a large box costs \$19

Solve each system by graphing.

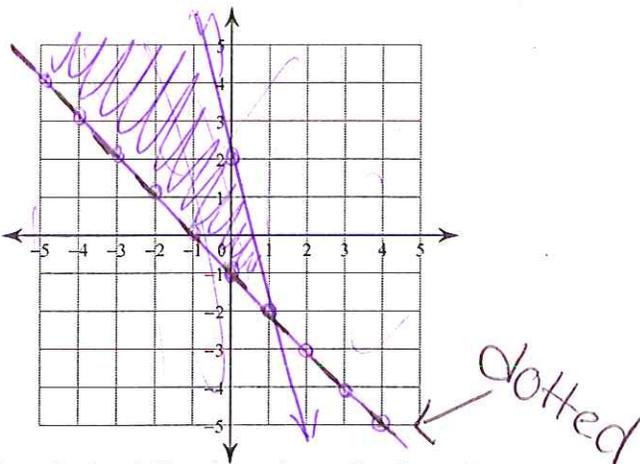
7) $y = -\frac{5}{3}x + 2$

$y = \frac{1}{3}x - 4$

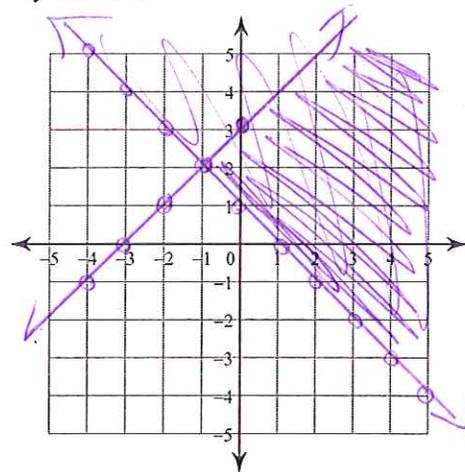


Sketch the solution to each system of inequalities.

8) $y \leq -4x + 2$
 $y > -x - 1$

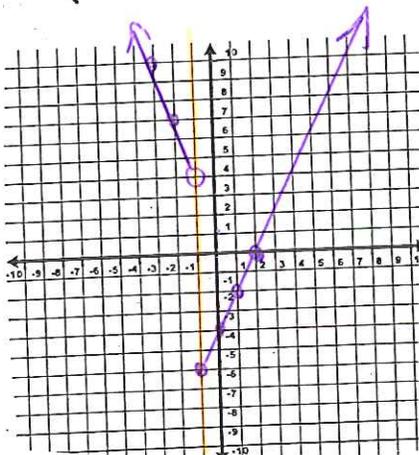


9) $y \geq -x + 1$
 $y \leq x + 3$

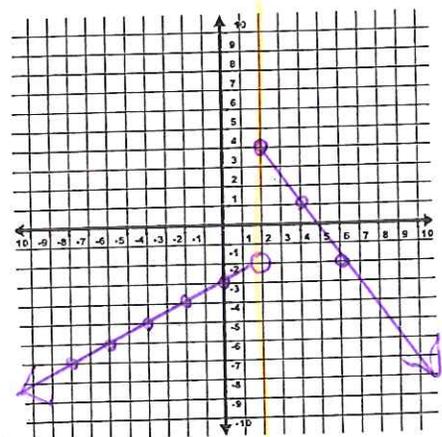


Graph the following piecewise function.

10) $f(x) = \begin{cases} -3x + 1 & \text{when } x < -1 \\ 2x - 4 & \text{when } x \geq -1 \end{cases}$



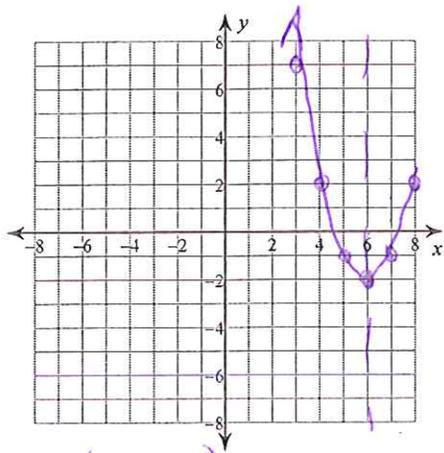
11) $f(x) = \begin{cases} \frac{1}{2}x - 3 & \text{when } x < 2 \\ -\frac{3}{2}x + 7 & \text{when } x \geq 2 \end{cases}$



Chapter 4 Review for FINAL

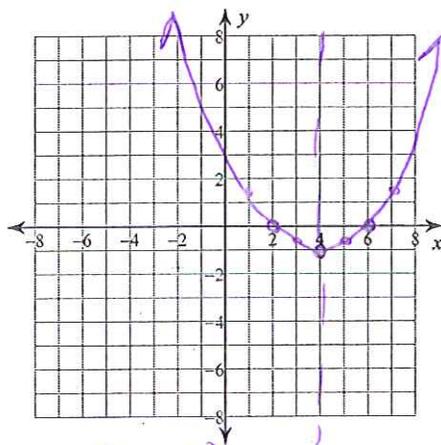
Identify the vertex, axis of symmetry, domain, range, and direction of opening of each. Then sketch the graph.

1) $y = (x - 6)^2 - 2$



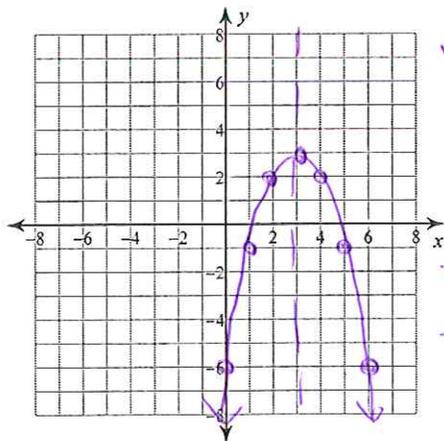
V: (6, -2)
 AOS: $x = 6$
 D: \mathbb{R} or $(-\infty, \infty)$
 R: $y \geq -2$ or $[-2, \infty)$
 Open: UP

2) $y = \frac{1}{4}(x - 4)^2 - 1$



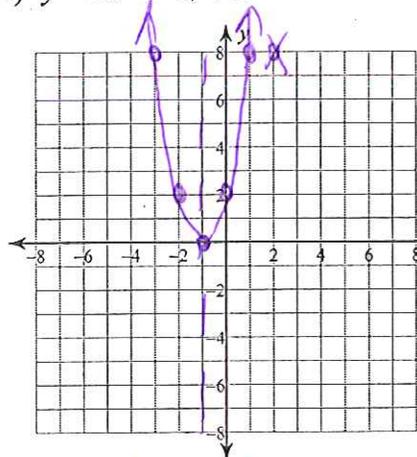
V: (4, -1)
 AOS: $x = 4$
 D: $(-\infty, \infty)$ or \mathbb{R}
 R: $[-1, \infty)$ or $y \geq -1$
 Open: UP

3) $y = -x^2 + 6x - 6$



$x = \frac{-b}{2a}$
 $x = \frac{6}{2(-1)}$
 $x = 3$
 $-(3)^2 + 6(3) - 6$
 $-9 + 18 - 6$
 V: (3, 3)
 AOS: $x = 3$
 D: $(-\infty, \infty)$ or \mathbb{R}
 R: $(-\infty, 3]$ or $y \leq 3$
 Open: down

4) $y = 2x^2 + 4x + 2$



$x = \frac{-4}{2(2)}$
 $x = -1$
 $y = 2(-1)^2 + 4(-1) + 2$
 $y = 2 - 4 + 2$
 $y = 0$
 V: (-1, 0)
 AOS: $x = -1$
 D: $(-\infty, \infty)$ or \mathbb{R}
 R: $[0, \infty)$ or $y \geq 0$
 Open: UP

Solve each equation by factoring.

5) $x^2 + 5x - 14 = 0$

$(x+7)(x-2) = 0$
 $x = -7, 2$

6) $3n^2 - 27n = -54$

$3n^2 - 27n + 54 = 0$
 $3(n^2 - 9n + 18) = 0$
 $3(n-6)(n-3) = 0$
 $n = 6, 3$

7) $15r^2 + 19r - 56 = 0$

Mult: -840
 Add: 19
 40, -21
 $(15r^2 + 40r)(-21r - 56) = 0$
 $5r(3r+8) - 7(3r+8) = 0$
 $(5r-7)(3r+8) = 0$
 $5r-7=0$ $3r+8=0$
 $r = 7/5, -8/3$

8) $3x^2 - 8x - 16 = 0$

Mult: -48
 Add: -8
 $(3x^2 - 12x) + (4x - 16) = 0$
 $3x(x-4) + 4(x-4) = 0$
 $(x-4)(3x+4) = 0$
 $x = 4, -4/3$

9) $6b^2 - 12b = 0$

$6b(b-2) = 0$
 $6b = 0$ $b-2 = 0$
 $b = 0, 2$

10) $6b^2 + 9 = 177$

$-9 - 9$
 $6b^2 = 168$
 $b^2 = 28$
 $b = \pm\sqrt{28}$
 $b = \pm 2\sqrt{7}$

Solve each equation by completing the square.

11) $v^2 - 20v - 79 = -10$

$v^2 - 20v + (-10)^2 = 69 + 100$
 $\sqrt{(v-10)^2} = \sqrt{169}$
 $v-10 = \pm 13$
 $+10$ $+10$
 $v = 23, -3$

Find all zeros.

12) $f(x) = 5x^2 - 24x - 5$

Mult: -25
 Add: -24
 -25, 1
 $(5x^2 - 25x) + (x - 5) = 0$
 $5x(x-5) + 1(x-5) = 0$
 $(5x+1)(x-5) = 0$
 $x = -1/5, 5$

Solve each equation with the quadratic formula.

13) $8m^2 + 11 = 8m$

$8m^2 - 8m + 11 = 0$
 $x = \frac{8 \pm \sqrt{(-8)^2 - 4(8)(11)}}{2(8)}$
 $x = \frac{8 \pm \sqrt{-288}}{16} \rightarrow \sqrt{+44} \cdot 2$

$x = \frac{8 \pm 12i\sqrt{2}}{16}$
 ~~$x = \frac{8 \pm 12i\sqrt{2}}{16}$~~
 $x = \frac{2 \pm 3i\sqrt{2}}{4}$

14) $10a^2 + 7 = 8a$

$10a^2 - 8a + 7 = 0$
 $x = \frac{8 \pm \sqrt{(-8)^2 - 4(10)(7)}}{2(10)}$
 $x = \frac{8 \pm \sqrt{-216}}{20}$
 $x = \frac{8 \pm 6i\sqrt{6}}{20}$
 $x = \frac{4 \pm 3i\sqrt{6}}{10}$

Simplify.

$$15) (-6 - 3i) + (5 - 8i)$$
$$-6 - 3i + 5 - 8i$$
$$\boxed{-1 - 11i}$$

$$17) (8i)(i)(-4 + 4i)$$

$$8i^2$$
$$-8(-4 + 4i)$$
$$\boxed{32 - 32i}$$

$$19) i^{15}$$

$$-i$$

$$16) (2 + 7i) - (7 - i)$$

$$2 + 7i - 7 + i$$
$$\boxed{-5 + 8i}$$

$$18) (7 + 4i)^2$$

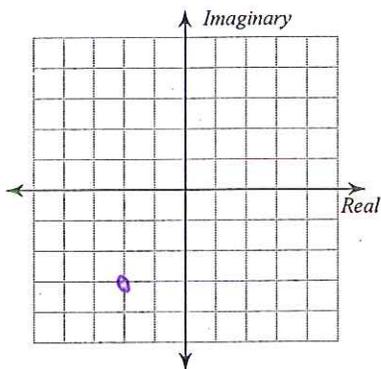
$$(7 + 4i)(7 + 4i) \quad (-1)$$
$$49 + 28i + 28i + 16i^2$$
$$\boxed{33 + 56i}$$

$$20) i^{99}$$

$$-i$$

Graph each number in the complex plane.

$$21) -2 - 3i$$



$$22) 2 - 2i$$

